Key Steps to Design an Interleaved PFC Stage Driven by the NCP1631

Interleaved PFC is an emerging solution that becomes particularly popular in applications where a strict form factor has to be met like for instance, in slim notebook adapters or in LCD TVs. Interleaving consists in paralleling two “small” stages in lieu of a bigger one, which may be more difficult to design. Practically, two 150-W PFC stages are combined to form our 300-W PFC pre-regulator. This approach has several merits like the ease of implementation, the use of more but smaller components or a better heat distribution.

Also, Interleaving extends the power range of Critical Conduction Mode (CrM) that is an efficient and cost-effective technique (no need for low trr diodes). Even, as reported by NCP1631EVB/D [3], when associated to the Frequency Clamped Critical conduction Mode (FCCrM), this technique yields particularly high efficiency levels (about 95% over a large load range at 90 Vrms in a 300-W application).

Furthermore, if the two stages are operated out-of-phase, the current ripple is significantly reduced. In particular, the input current looks like that of a Continuous Conduction Mode (CCM) one and the rms current within the bulk capacitor is dramatically reduced. These characteristics are detailed in application note AND8355 [1].

This paper gives the main equations that are useful to design an interleaved PFC stage driven by the NCP1631. The process is illustrated by the following 300-W, universal mains application:

- Maximum Output Power: 300 W
- Input Voltage Range: from 90 Vrms to 265 Vrms
- Regulation Output Voltage: 390 V

The computations relevant to the power components are based on the assumption that the current is perfectly shared between the two branches. This assumption is valid if the two coil inductances properly match [2].

Figure 1. Generic Application Schematic
INTRODUCTION

The NCP1631 integrates a dual MOSFET driver for interleaved, 2-phase PFC applications. It drives the two branches in so-called Frequency Clamped Critical conduction Mode (FCCrM) where each phase operates in Critical conduction Mode (CrM) in the most stressful conditions and in Discontinuous Conduction Mode (DCM) otherwise, acting as a CrM controller with a frequency clamp (given by the oscillator). According to the conditions, the PFC stage actually jumps from DCM to CrM (and vice versa) with no discontinuity in operation and without degradation of the current shape.

Furthermore, the circuit incorporates protection features for a rugged operation together with some special circuitry to lower the power consumed by the PFC stage in no-load conditions. More generally, the NCP1631 is ideal in systems where cost-effectiveness, reliability, low stand-by power and high power factor are the key parameters:

Fully Stable FCCrM and Out-Of-Phase Operation

Unlike master/slave controllers, the NCP1631 utilizes an interactive-phase approach where the two branches operate independently. Hence, the two phases necessarily operate in FCCrM, preventing risks of undesired dead-times or continuous conduction mode sequences. In addition, the circuit makes them interact so that they run out-of-phase. The NCP1631 unique interleaving technique substantially maintains the wished 180° phase shift between the 2 branches, in all conditions including start-up, fault or transient sequences.

Optimized Efficiency Over the Full Power Range

The NCP1631 optimizes the efficiency of your PFC stage in the whole line/load range. Its clamp frequency is a major contributor at nominal load. For medium and light load, the clamp frequency linearly decays as a function of the power to maintain high efficiency levels even in very light load. The power threshold under which frequency reduces is programmed by the resistor placed between pin 6 and ground. To prevent any risk of regulation loss at no load, the circuit further skips cycles when the error amplifier reaches its low clamp level.

Fast Line/Load Transient Compensation

Characterized by the low bandwidth of their regulation loop, PFC stages exhibit large over and under-shoots when abrupt load or line transients occur (e.g. at start-up). The NCP1631 dramatically narrows the output voltage range. First, the controller dedicates one pin to set an accurate Over-Voltage Protection level and interrupts the power delivery as long as the output voltage exceeds this threshold. Also, the NCP1631 dynamic response enhancer drastically speeds-up the regulation loop when the output voltage is 4.5% below its desired level. As a matter of fact, a PFC stage provides the downstream converter with a very narrow voltage range.

A “pfcOK” Signal

The circuit detects when the PFC stage is in steady state or if on the contrary, it is in a start-up or fault condition. In the first case, the “pfcOK” pin (pin15) is in high state and low otherwise. This signal is to disable the downstream converter unless the bulk capacitor is charged and no fault is detected. Finally, the downstream converter can be optimally designed for the narrow voltage provided by the PFC stage in normal operation.

Safety Protections

The NCP1631 permanently monitors the input and output voltages, the input current and the die temperature to protect the system from possible over-stresses and make the PFC stage extremely robust and reliable. In addition to the aforementioned OVP protection, one can list:

Maximum Current Limit:
The circuit permanently senses the total input current and prevents it from exceeding the preset current limit, still maintaining the out-of-phase operation.

In-rush Detection:
The NCP1631 prevents the power switches turn on for the large in-rush currents sequence that occurs during the start-up phase.

Under-Voltage Protection:
This feature is mainly to prevent operation in case of a failure in the OVP monitoring network (e.g., bad connection).

Brown-Out Detection:
The circuit stops operating if the line magnitude is too low to protect the PFC stage from the excessive stress that could damage it in such conditions.

Thermal Shutdown:
The circuit stops pulsing when its junction temperature exceeds 150°C typically and resumes operation once it drops below about 100°C (50°C hysteresis).
Defining the oscillator frequency of the NCP1631 is a prerequisite step before dimensioning the PFC stage. In the presented application, we choose to clamp the switching frequency at around 120 kHz in each phase, because this frequency is generally a good trade-off when considering the following aspects:

- A high switching frequency reduces the size of the storage elements. In particular, it is well known that the higher the switching frequency, the lower the inductor core. That is why, one should set the switching frequency as high as possible,
- On the other hand, increasing the switching frequency has two major drawbacks:

  1. The switching rate increasing, the associated losses grow up. In addition, all parasitic capacitors charge at a higher frequency and generate more heat...
  2. EMI filtering is tougher: the switching generates high EMI rays at the switching frequency and close harmonic levels. Most power supplies have to meet the CISPR22 standard that applies to frequencies above 150 kHz. That is why SMPS designers often select 130 kHz so that the fundamental keeps below 150 kHz and then out of the regulation scope. Often, 65 kHz is also chosen to not to have to damp harmonic 2 too.

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\[ L \geq \frac{(V_{in, rms})_{LL}^2 \cdot (V_{out} - \sqrt{2}) \cdot (V_{in, rms})_{LL}}{(P_{in, avg})_{max} \cdot V_{out, nom} \cdot f_{sw(max)}} \quad (eq. 3) \]

In our application, this leads to:

\[ L \geq \frac{90^2 \cdot (390 - \sqrt{2} \cdot 90)}{325 \cdot 390 \cdot 120 \cdot 10^3} \approx 139 \mu H \quad (eq. 4) \]

Finally, a 150 µH/6 A pk/2.5 A rms coil was selected.

**Power Semiconductors**

The bridge diode should be selected based on the peak current rating and the power dissipation given by:

\[ P_{bridge} = \frac{4 \cdot \sqrt{2} \cdot V_f \cdot (P_{in, avg})_{max}}{(V_{in, rms})_{LL}} \approx 1.8 \cdot V_f \cdot \frac{325}{90} \approx 6.5 \cdot V_f \quad (eq. 5) \]

Assuming a 1-V forward voltage per diode (\(V_f = 1 \text{ V}\)), the bridge approximately dissipates 6.5 W.

For each branch, the MOSFET is selected based on the peak voltage stress (\(V_{out(max)} + \text{margin}\)) and on the rms current flowing through it (\(I_{M(rms)}\)):

\[ I_{M(rms)} = \frac{\sqrt{2}}{3} \cdot \frac{(P_{in, avg})_{max}}{(V_{in, rms})_{LL}} \cdot \sqrt{1 - \frac{8 \cdot \sqrt{2} \cdot (V_{in, rms})_{LL}}{3 \cdot \pi \cdot V_{out, nom}}} = \frac{325}{90} \cdot \sqrt{1 - \frac{8 \cdot \sqrt{2} \cdot 90}{3 \cdot \pi \cdot 390}} \approx 1.8 \text{ A} \quad (eq. 6) \]

Using a 600-V, 0.4-Ω FET (SPP11N60), will give conduction losses of (assuming that \(R_{DS(on)}\)) increases by 80% due to temperature effects:

\[ P_{cond} = I_{M(rms)}^2 \cdot R_{DS(on)} = 1.8^2 \cdot 0.4 \cdot 1.8 \approx 2.3 \text{ W} \quad (eq. 7) \]
This computation is valid for one branch. As there are two phases to consider, the total MOSFETs conduction losses are actually twice (4.6 W).

Switching losses are hard to predict. They are not computed here. As a rule of the thumb, we generally reserve a loss budget equal to that of the conduction ones. One can anyway note that the NCP1631 limits this source of dissipation by clamping the switching frequency (that can never exceed the oscillator one – 120 kHz in each branch in our case). To further improve the efficiency, the MOSFET opening can be accelerated using the schematic of Figure 2, where the Q1 small npn transistor (TO92) amplifies the MOSFET turn off gate current.

![Figure 2. Q1 Speeds Up the MOSFET Turn Off](image)

The input bridge that rectifies the line voltage and the MOSFETs of the two branches share the same heat-sink.

Based on above computations, the total power to be dissipated is in the range of: \((6.5 + 4.6 + 4.6 \approx 16 \text{ W})\). A 2.9°C/W heat-sink (ref. 437479 from AAVID THERMALLOY) is implemented. It limits the rise of the case temperature (of the input bridge and MOSFETs applied to it) to about 50° compared to the ambient temperature.

Interleaved PFC requires two boost diodes (one per branch). No reverse recovery issues to worry about. Simply, they must meet the correct voltage rating \((V_{\text{out(max)}} + \text{margin})\) and exhibit a low forward voltage drop. Supposing a perfect current sharing, the average diode current is the half of the load one:

\[
\left( I_{D1(\text{avg})} = I_{D2(\text{avg})} = \frac{I_{\text{LOAD}}}{2} = \frac{P_{\text{out}}}{2 \cdot V_{\text{out}}} = 0.39 \text{ A} \right)
\]

So, the losses are about

\[
\left( \frac{I_{\text{LOAD}} \cdot V_{\text{f}}}{2} \right)
\]

per diode, i.e., less than 500 mW per diode using MUR550 rectifiers. For each phase, the peak current seen by the diode will be the same as the corresponding inductor peak current. Two axial MUR550 are selected.

### Bulk Capacitor Design

The output capacitor is generally designed considering three factors:

1. The maximum permissible low frequency ripple of the output voltage. The input current and voltage being both sinusoidal, PFC stages deliver a squared sinusoidal power that matches the load power demand in average only. As a consequence, the output voltage exhibits a low frequency ripple (e.g., 100 Hz ripple in Europe or 120 Hz in USA) that is inherent to the PFC function.

2. The rms magnitude of the current flowing through the bulk capacitor. Based on this computation, one must estimate the maximal permissible ESR not to cause an excessive heating.

3. The hold-up time. It can be specified that the power supply must provide the full power for a short mains interruption that is the so called hold-up time. The hold-up time is generally in the range of 10 or 20 ms.

The output voltage ripple is given by:

\[
\Delta V_{\text{out(p-p)}} = \frac{P_{\text{out}}}{2 \pi \cdot f_{\text{line}} \cdot C_{\text{bulk}} \cdot V_{\text{out,nom}}} \quad (\text{eq. 8})
\]

The capacitor rms current is given by (assuming a resistive load):

\[
I_{C(\text{rms})} = \sqrt{\frac{16 \cdot \frac{5}{2} \cdot P_{\text{out}}^2}{9 \cdot \pi \cdot (V_{\text{in(rms)}})^2 \cdot V_{\text{out}} \cdot \eta^2 - \left( \frac{\eta^2}{V_{\text{out,nom}}} \right)^2}} \quad (\text{eq. 9})
\]

Finally the following equation expresses the hold-up time:

\[
\text{t}_{\text{hold-up}} = \frac{C_{\text{bulk}} \cdot (V_{\text{out}}^2 - V_{\text{out(min)}}^2)}{2 \cdot P_{\text{out}}} \quad (\text{eq. 10})
\]

Where \(V_{\text{out(min)}}\) is the minimal bulk voltage necessary to the downstream converter to keep properly feeding the load.

The hold-time being not considered here, a 100-µF capacitor was chosen to satisfy the other above conditions. The peak-peak ripple is 25 V (±3% of \(V_{\text{out}}\)) and the rms current is 1.4 A.
The NCP1631 clamps the maximum frequency of the PFC stage without power factor degradation. This feature prevents the switching frequency from reaching excessive levels at light load. As detailed in the NCP1631 data sheet, the clamp frequency in each phase is actually half the oscillator one.

Hence:

\[ f_{\text{sw(max)}} = \frac{f_{\text{osc}}}{2} \quad \text{(eq. 11)} \]

Where:

- \( f_{\text{sw(max)}} \) is the frequency clamp for the first branch of the interleaved PFC and \( f_{\text{sw(max)}} \) of the second one being equal, \( f_{\text{sw(max)}} \) stands for the clamp frequency for any of the two phases.
- \( f_{\text{osc}} \) is the oscillator frequency.

In the absence of frequency foldback (heavy load in general), the oscillator swings at its nominal frequency \( f_{\text{osc(nom)}} \) and each branch operates with a nominal clamp frequency \( f_{\text{sw(max)}} \) given by:

\[ (f_{\text{sw(max)}})_{\text{nom}} = \frac{f_{\text{osc(nom)}}}{2} \approx \frac{26 \cdot 10^{-6}}{C_{\text{pin4}}} \quad \text{(eq. 12)} \]

For instance, a 220-pF capacitor leads to the following clamp frequency:

\[ (f_{\text{sw(max)}})_{\text{nom}} \approx \frac{26 \cdot 10^{-6}}{220 \cdot 10^{-9}} = 118 \text{ kHz} \quad \text{(eq. 13)} \]

**Frequency Fold-back**

The NCP1631 features the frequency fold-back function to improve the light load efficiency. Practically, the oscillator charge and discharge currents are not constant but proportional to power when the load drops below a programmable level, as shown by Figure 3.

![Figure 3. Frequency Fold-back](http://onsemi.com)

\[ f_{\text{osc(nom)}} = 118 \text{ kHz} \]

**Programming the Power Threshold for Frequency Fold-back**

Pin6 of the NCP1631 pins out the signal \( V_{\text{REGUL}} \) that is proportional to the power that is delivered. The resistor \( R_{FF} \) placed between pin 6 and ground, adjusts the pin6 current \( I_{FF} \) as follows:

\[ I_{FF} = \begin{cases} \frac{V_{\text{REGUL}}}{R_{FF}} & \text{if } V_{\text{REGUL}} \leq 105 \mu \text{A} \\ 105 \mu \text{A} & \text{otherwise} \end{cases} \]

As a matter of fact, the clamp frequency is also an increasing function of \( V_{\text{REGUL}} \) until it reaches a maximum value \( f_{\text{osc(nom)}} = 105 \mu \text{A} \):

\[ f_{\text{osc}} = f_{\text{osc(nom)}} \quad \text{if } V_{\text{REGUL}} \geq R_{FF} \cdot 105 \mu \text{A} \]

\[ f_{\text{osc}} = \frac{V_{\text{REGUL}}}{R_{FF} \cdot 105 \mu} \cdot f_{\text{osc(nom)}} \quad \text{if } V_{\text{REGUL}} \leq R_{FF} \cdot 105 \mu \text{A} \]

\( V_{\text{REGUL}} \) varies between 0 and 1.66 V. Since the power that can be delivered is proportional to \( V_{\text{REGUL}} \), the power threshold for frequency fold-back is:

\[ (P_{\text{in}})_{FF} = \frac{R_{FF} \cdot 105 \mu \text{A}}{1.66 \text{ V}} \cdot (P_{\text{in}})_{HL} \approx \frac{R_{FF}}{15 \cdot 810} \cdot (P_{\text{in}})_{HL} \quad \text{(eq. 14)} \]

Where:

- \( (P_{\text{in}})_{FF} \) is the input power below which the frequency reduces.
- \( (P_{\text{in}})_{HL} \) is the power highest level that can virtually be delivered by the PFC stage. This value results from the timing resistor selection (see the “maximum power adjustment” section) and is generally set 25% or 30% higher than the application maximum power to offer some margin.
In our application, a 4.7-kΩ resistor is implemented on pin 6 (R_{FF} = 4.7 kΩ). Hence, the frequency folds back when the input power drops below the following (P_{in})_{FF} threshold:

\[
(P_{in})_{FF} = \frac{4.7 \cdot 10^3}{15.810} \cdot (P_{in})_{HL} \approx 30\% \cdot (P_{in})_{HL} \quad (eq. 15)
\]

In our application, the maximum input power is 325 W. It is recommended to design the PFC stage so that it can produce at least 25% more than the maximum power it targets. In practice, ((P_{in})_{HL} = 494 W) has been selected. As a matter of fact, the frequency folds back when the input power goes below (30\% \cdot (P_{in})_{HL}) that is about 147 W.

### Forcing a Minimum Frequency

The NCP1631 reduces the frequency down to virtually zero. As detailed in the data sheet and shown by the simplified oscillator representation of Figure 4, the circuit lowers the frequency by diminishing the I_{FF} current. When this current is near zero, a 35-μA current source is still available for charging the oscillator capacitor but the discharge current is near zero leading to an extremely long discharge time and a very low frequency.

It is wise to prevent the frequency from dropping below 16 kHz to avoid audible noise issues. A simple means consists of placing a resistor (R_{Fmin}) between the “OSC” pin and ground to force a minimum oscillator discharge current (see Figure 4).

### Assuming that the internal I_{FF} current is zero, the oscillator period can be computed considering the 35-μA charge current, the permanent leakage current generated by R_{Fmin} and the 1 V swing across C_{OSC} (swing when the oscillator is clamping the switching frequency).

Doing this calculation, we can deduce the minimum clamp frequency (for each branch) forced by R_{Fmin}:

\[
(f_{sw(max)})_{min} = \frac{f_{OSC(min)}}{2} = \frac{1}{2 \cdot R_{Fmin} \cdot C_{OSC} \cdot \left(0.22 + \ln\left(\frac{R_{Fmin}}{R_{Fmin}}\right)\right)} \quad (eq. 16)
\]

In our application, (R_{Fmin} = 270 kΩ) forces a minimum frequency of about 20 kHz.

### Remark:

Ground pin6 to inhibit the frequency foldback. If pin6 is grounded (accidently or not), the circuit operates with the nominal clamp frequency over the whole load range.
BROWN-OUT CIRCUITRY

The brown-out terminal (pin7) typically receives a portion of the PFC input voltage ($V_{IN}$). As during the PFC operation, $V_{IN}$ is a rectified sinusoid, a capacitor must integrate the ac line ripple so that a portion of the ($V_{IN}$) average value is applied to the brown-out pin.

![Diagram of brown-out circuitry]

Figure 5. Brown-out Block
As sketched by Figure 5, the brown-out block has two functions:

1. Feed-forward: The brown-out pin voltage is buffered to generate an internal current $I_{BO}$ proportional to the input voltage average value in conjunction with the pin3 resistor ($R_t$). This current is squared to form the current that charges the internal timing capacitors that control the on-time in the two branches. As a matter of fact, the on-time is inversely proportional to the square of the line magnitude. This feed-forward feature makes the transfer function and the power delivery independent of the ac line level.

2. Detection of the line magnitude being too low. A current source lowers the BO pin voltage when a brown-out condition is detected, for hysteresis purpose as required by this function. In traditional applications, the sensed voltage dramatically varies depending on the PFC stage state:
   - Before operation, the PFC stage is off and the input bridge acts as a peak detector (refer to Figure 6). As a consequence, the input voltage is approximately flat and nearly equates the ac line amplitude:
     \[ V_{in} = \sqrt{2} \cdot V_{in,rms} \]
     where $V_{in,rms}$ is the rms voltage of the line. Hence, the voltage applied to pin 7 is:
     \[ V_{pin7} = \frac{\sqrt{2} \cdot V_{in,rms}}{\pi} \cdot \frac{R_{bo2}}{R_{bo1} + R_{bo2}} \]
   - After the PFC stage has started operation, the input voltage becomes a rectified sinusoid and the voltage applied to pin 7 is:
     \[ V_{pin7} = \frac{2 \cdot \sqrt{2} \cdot V_{in,rms}}{\pi} \cdot \frac{R_{bo2}}{R_{bo1} + R_{bo2}} \]
     i.e., about 64% of the previous value.

Therefore, in traditional applications, the same line magnitude leads to a BO pin voltage that is 36% lower when the PFC is working. That is why a large hysteresis is required.

\[ f_{BO} = \frac{R_{bo1} + R_{bo2}}{2\pi \cdot R_{bo1} \cdot R_{bo2} \cdot C_{bo}} \]

**Figure 6. Typical Input Voltage of a PFC Stage**

**Computing $C_{bo}$, $R_{bo1}$ and $R_{bo2}$ of Figure 5**

1. Define the line levels at which the circuit should detect a brown-out and recover operation:
   - The system starts operating when the line voltage is above ($V_{in,rms}$)$_{boH} = 81$ V (90% of 90 V)
   - The system detects a fault when the line voltage goes below ($V_{in,rms}$)$_{boL} = 72$ V (80% of 90 V)

2. Define the average input voltage when $V_{pin7}$ (BO pin voltage) crosses the BO thresholds ($V_{pin7}$ rising and falling):

When the line voltage is below the BO threshold, the internal current source ($I_{HYST} = 7 \mu A$ typically) is activated to offer some hysteresis and the circuit recovers operation when:

\[ \frac{R_{bo2}}{R_{bo1} + R_{bo2}} \cdot (V_{in,avg})_{boH} - \left( \frac{R_{bo1} \cdot R_{bo2}}{R_{bo1} + R_{bo2}} \cdot I_{HYST} \right) = V_{bo(th)} \]  
(eq. 17)

Where ($V_{in,avg}$)$_{boH}$ is the average input voltage above which the circuit turns on and $V_{bo(th)}$ is the BO internal threshold (1 V typically).

Hence:

\[ (V_{in,avg})_{boH} = \left( \frac{R_{bo1} + R_{bo2}}{R_{bo2}} \cdot V_{bo(th)} \right) + \left( R_{bo1} \cdot I_{HYST} \right) \]  
(eq. 18)

As long as the line is above the BO threshold, the internal current source ($I_{HYST} = 7 \mu A$ typically) is off and the BO pin voltage is:

\[ V_{pin7} = k_{BO} \cdot V_{in,avg} \cdot \left( 1 - \frac{f_{BO}}{3 \cdot f_{line}} \right) \]  
(eq. 19)

Where:

- ($V_{in,avg}$) is the average input voltage
- $f_{line}$ is the line frequency
- $f_{BO}$ is the sensing network pole frequency
k_{BO} is scale down factor of the BO sensing network

\[ k_{BO} = \frac{R_{bo2}}{R_{bo1} + R_{bo2}} \]

The term

\[ \left(1 - \frac{f_{BO}}{3 \cdot f_{line}}\right) \]

of Equation 19 enables to take into account the BO pin voltage ripple (first harmonic approximation).

A brown-out fault is detected when the BO pin voltage goes below \( V_{bo(th)} \) (BO internal threshold that is 1 V typically). Hence, the BO protection triggers when the average voltage goes below the \((V_{in,avg})_{boL}\) level expressed by the following equation:

\[ (V_{in,avg})_{boL} = \frac{V_{BO(th)}}{k_{BO} \cdot \left(1 - \frac{f_{BO}}{3 \cdot f_{line}}\right)} \quad (eq. 20) \]

Where \((V_{in,avg})_{boL}\) is the average input voltage below which the circuit turns off, \(f_{BO}\) is the sensing network pole frequency

\[ f_{BO} = \frac{R_{bo1} + R_{bo2}}{2\pi \cdot R_{bo1} \cdot R_{bo2} \cdot C_{bo}} \]

and \(f_{line}\) is the line frequency.

3. Calculation:

From Equation 20, we can deduce the following expression of the brown-out scale down factor:

\[ K_{BO} = \frac{R_{bo2}}{R_{bo1} + R_{bo2}} = \frac{V_{BO(th)}}{(V_{in,avg})_{boL} \cdot \left(1 - \frac{f_{BO}}{3 \cdot f_{line}}\right)} \quad (eq. 21) \]

Substitution of Equation 21 into Equation 18 leads to:

\[ (V_{in,avg})_{boH} = \left(\frac{(V_{in,avg})_{boL} \cdot \left(1 - \frac{f_{BO}}{3 \cdot f_{line}}\right)}{V_{BO(th)}}\right) + [R_{bo1} \cdot I_{HYST}] \]

We can then deduce the following expression of \(R_{bo1}\):

\[ R_{bo1} = \frac{I_{HYST}}{\left(\frac{(V_{in,avg})_{boL} \cdot \left(1 - \frac{f_{BO}}{3 \cdot f_{line}}\right)}{V_{BO(th)}}\right) - 1} \quad (eq. 23) \]

Re-using the above \(R_{bo1}\) expression, one can deduce \(R_{bo2}\) from Equation 21:

\[ R_{bo2} = \frac{R_{bo1}}{\left(\frac{(V_{in,avg})_{boL} \cdot \left(1 - \frac{f_{BO}}{3 \cdot f_{line}}\right)}{V_{BO(th)}}\right) - 1} \]

If as a rule of the thumb, we will assume that

\[ f_{BO} = \frac{f_{line}}{10} \]

that is 6 Hz in the case of a 60-Hz line, we obtain:

As an example, we will consider the traditional PFC stage where the average value of the input voltage is 36% lower when the circuit operates (as illustrated by Figure 6).

So if we select:

- The system starts operating when the line voltage is above
  \( (V_{in,avg})_{boH} = 81 \text{ V} \)

- The system detects a fault when the line voltage goes below
  \( (V_{in,avg})_{boL} = 72 \text{ V} \)

The corresponding average input voltage thresholds are:

\[ (V_{in,avg})_{boH} = \sqrt{2} \cdot (V_{in,avg})_{boL} = \sqrt{2} \cdot 81 \quad (eq. 27) \]

And:

\[ (V_{in,avg})_{boL} = \frac{2}{\sqrt{2}} \cdot (V_{in,avg})_{boL} = \frac{2}{\sqrt{2}} \cdot 72 \quad (eq. 28) \]

We have then to solve:

\[ R_{bo1} = \frac{I_{HYST}}{7 \cdot 10^{-6} - 0.967 \cdot \frac{2}{\sqrt{2}} \cdot 72} = 7410 \text{ k}\Omega \quad (eq. 29) \]

\[ R_{bo2} = \frac{7410 \cdot 10^3}{0.967 \cdot \frac{2}{\sqrt{2}} \cdot 72 - 1} \approx 120 \text{ k}\Omega \quad (eq. 30) \]
\[ C_{bo} = \frac{R_{bo1} + R_{bo2}}{2\pi \cdot R_{bo1} \cdot R_{bo2} \cdot \frac{l_{line}}{10}} = \frac{7410 \, k + 120 \, k \cdot \frac{60}{10}}{2\pi} \quad (eq. \, 31) \]

In practice, four 1.8-M\(\Omega\) resistors are placed in series for \(R_{bo1}\) (for a global 7.2-M\(\Omega\) resistor) and we use a 120-k\(\Omega\) resistor for \(R_{bo2}\) and 220-nF capacitor for \(C_{bo}\).

One should note that the NCP1631 brown-out circuitry incorporates a 50-ms blanking delay to help meet hold-up times requirement (see data sheet).

**MAXIMUM POWER ADJUSTMENT**

The instantaneous line current is the averaged value (over the switching frequency) of the total current absorbed by the two branches of the PFC stage. It is given by the following formula:

\[
I_{in}(t) = \frac{V_{in}(t)}{L} \cdot \frac{(R_t)^2 \cdot V_{REGUL}}{26.9 \cdot 10^{12} \cdot k_{BO}^2 \cdot V_{in,rms}^2} \quad (eq. \, 32)
\]

Where:

\[
\left( \frac{(R_t)^2 \cdot V_{REGUL}}{26.9 \cdot 10^{12} \cdot k_{BO}^2 \cdot V_{in,rms}^2} \right)
\]

is the expression of the on-time in each branch

- \((V_{REGUL})\) is an internal signal linearly dependent of the output of the regulation block (VCONTROL). \((V_{REGUL})\) varies between 0 and 1.66 V.
- \(I_{in}(t)\) and \(V_{in}(t)\) are the instantaneous line current and voltage respectively.
- \(V_{in,rms}\) is the line rms voltage
- \(L\) is the coil inductance
- \(k_{BO}\) is scale down factor of the BO sensing network

Multiplying \(I_{in}\) by \(V_{in}\), one can deduce the instantaneous power:

\[
P_{in}(t) = \frac{(R_t)^2 \cdot V_{REGUL} \cdot V_{in}^2(t)}{26.9 \cdot 10^{12} \cdot L \cdot k_{BO}^2 \cdot V_{in,rms}^2} \quad (eq. \, 33)
\]

And averaging the instantaneous power over the line period gives the following expression of the mean input power:

\[
P_{in,avg} = \frac{(R_t)^2 \cdot V_{REGUL}}{26.9 \cdot 10^{12} \cdot L \cdot k_{BO}^2} \quad (eq. \, 34)
\]

As a result of the feed-forward, the delivered power does not depend on the line magnitude but is the only function of the coil inductance, of the input voltage sensing network (used and dimensioned for the brown-out detection) and of \(R_t\) capacitor, that is, the timing resistor that is applied to pin3.

Since \(V_{REGUL}\) is clamped to 1.66 V, the maximum power \(((P_{in})_{HL})\) that can be virtually delivered by the PFC stage is:

\[
(P_{in})_{HL} = \frac{(R_t)^2 \cdot 1.66}{26.9 \cdot 10^{12} \cdot L \cdot k_{BO}^2} \quad (eq. \, 35)
\]

Hence:

\[
R_t \approx 4025 \cdot 10^3 \cdot k_{BO} \cdot \sqrt{\frac{L \cdot (P_{in})_{HL}}{16.2 \cdot 10^{12} \cdot L \cdot k_{BO}^2}} \quad (eq. \, 36)
\]

For the sake of a welcome margin, \(((P_{in})_{HL})\) should be selected about 25% higher than the expected maximal input power that is: \((125\% \times 325 \, W = 400 \, W)\) in the application of interest.

In our case,

- \(L = 150 \, \mu H\)
- Since \(R_{bo1} = 7,200 \, k\Omega\) and \(R_{bo2} = 120 \, k\Omega\),

\[
k_{BO} = \frac{R_{bo2}}{R_{bo1} + R_{bo2}} = \frac{1}{61}
\]

Hence:

\[
R_t \approx 4025 \cdot 10^3 \cdot \frac{1}{61} \cdot \sqrt{150 \cdot 10^{-6} \cdot 400} \approx 16 \cdot 2 \, k\Omega
\]

A 18-k\(\Omega\) resistor is selected that leads to

\[
(P_{in})_{HL} = \frac{(18 \cdot 10^3)^2 \cdot 61^2}{16.2 \cdot 10^{12} \cdot 150 \cdot 10^{-6}} \approx 496 \, W
\]
The NCP1631 embeds a trans-conductance error amplifier that typically features a 200-μS trans-conductance gain and a ±20-μA maximum capability (see Figure 7). The output voltage of the PFC stage is externally scaled down by a resistors divider and monitored by the feed-back input (pin2). The bias current is minimized (less than 500 nA) to allow the use of a high impedance feed-back network. The output of the error amplifier is pinned out for external loop compensation (pin5).

**Computation of the Feed-back/Regulation External Components**

A resistor divider consisting of \( R_{b1} \) and \( R_{b2} \) of Figure 7 must provide pin2 with a voltage proportional to the PFC output voltage so that \( V_{pin2} \) equates the internal reference voltage (\( V_{REF} = 2.5 \) V) when the PFC output voltage is nominal. In other words:

\[
\frac{R_{b2}}{R_{b1} + R_{b2}} \cdot V_{out,nom} = V_{REF} \quad \text{(eq. 38)}
\]

Or:

\[
R_{b1} = \frac{V_{out,nom}}{V_{REF}} - 1 \quad \text{(eq. 39)}
\]

Another constraint on the feed-back resistors is the power it dissipates. \( R_{b1} \) and \( R_{b2} \) being biased by the PFC output high voltage (in the range of 390 V typically), they can easily consume several hundreds of mW if their resistance is low. Targeting a bias current in the range of 100 μA generally gives a good trade-off between losses and noise immunity.

This criterion leads to:

\[
R_{b2} = \frac{V_{REF}}{100 \mu A} = 25 \text{ kΩ} \quad \text{(eq. 40)}
\]

In practice, \( (R_{b2} = 27 \text{ kΩ}) \) was selected for our application. Following Equation 39, \( R_{b1} \) is given by:

\[
R_{b1} = R_{b2} \cdot \left( \frac{V_{out,nom}}{V_{REF}} - 1 \right) \quad \text{(eq. 41)}
\]

We target a 390-V regulation level, hence:

\[
R_{b1} = 27 \text{ kΩ} \cdot \left( \frac{390}{2.5} - 1 \right) = 4185 \text{ kΩ} \quad \text{(eq. 42)}
\]

Like for the input voltage sensing network, several resistors should be placed in series instead of a single \( R_{b1} \) resistor. In our application, we choose a \((1,800 \text{ kΩ} + 1,800 \text{ kΩ} + 560 \text{ kΩ})\) network. This selection together with \( (R_{b2} = 27 \text{ kΩ}) \) leads to:

\[
V_{out,nom} = \frac{R_{b1} + R_{b2}}{R_{b2}} \cdot V_{REF} \quad \text{(eq. 43)}
\]

\[
= \frac{1800 k + 1800 k + 560 k + 27 k}{27 k} \cdot 2.5 \text{ V} 
\]

\[
= 388 \text{ V} \quad \text{(eq. 44)}
\]

**Compensation**

The NCP1631 uses the brown-out input voltage to provide some feed-forward. This allows the small-signal transfer function of PFC stage to be independent of the ac line amplitude. More specifically, the bulk capacitor ESR being neglected:

\[
\frac{\dot{V}}{V_{REGUL}} = \frac{(R_{b})^2 \cdot R_{out}}{53.8 \cdot 10^{12} \cdot L \cdot k_{BO}^2 \cdot V_{out,nom} \cdot \left( 1 + \frac{R_{out} \cdot C_{bulk}}{s^2} \right)} \quad \text{(eq. 44)}
\]

Where:

- \( C_{bulk} \) is the bulk capacitor
- \( R_{out} \) is the load equivalent resistance
- \( R_{b} \) is the pin3 external capacitor
- \( L \) is the PFC coil inductance
- \( k_{BO} \) is the brown-out scale-down factor
- \( V_{out,nom} \) is the regulation level of the PFC output

However, PFC stages must exhibit a very low regulation bandwidth, in the range of or lower than 20 Hz to yield high power factor ratios. Hence, sharp variations of the load generally result in excessive over and under-shoots. The NCP1631 limits over-shoots by the Over-Voltage Protection (see OVP section). To contain under-shoots, an internal comparator monitors the feed-back \((V_{pin2})\) and when \( V_{pin2} \) is lower than 95.5% of its nominal value, it connects a 220-μA current source to speed-up the charge of the compensation capacitors. Finally, it is like if the comparator multiplied the error amplifier gain by about 10 (Note 1).

The implementation of this **dynamic response enhancer** together with the accurate and programmable over-voltage protection, guarantees a reduced spread of the output voltage in all conditions included sharp line/load transients.

Hence, in most applications, it can be sufficient to place a low frequency pole that drastically limits the bandwidth. However, it is recommended to implement a type2 compensation as represented by the following figure:

---

1. The circuit disables this capability (dynamic response enhancer) until the PFC stage output voltage has reached its target level (that is when the "pfcOK" signal of the block diagram, is high). This is because, at the beginning of operation, the pin5 compensation network must charge slowly and gradually for a soft-startup.
The output to control transfer function brought by the type-2 compensator is:

\[ \frac{V_{\text{control}}}{V_{\text{out}}} = \frac{1 + sR_z C_z}{s R_0 (C_z + C_p) \left( 1 + s R_z \frac{C_z \cdot C_p}{C_z + C_p} \right)} \]  

(eq. 45)

Where:

\[ R_0 = \frac{V_{\text{out,nom}}}{V_{\text{ref}} \cdot G_{\text{EA}}} \]

\[ G_{\text{EA}} \] being the gain of the trans-conductance error amplifier (OTA), \[ V_{\text{out,nom}} \], the output nominal voltage (\[ V_{\text{out}} \] regulation level) and \[ V_{\text{REF}} \], the OTA 2.5-V voltage reference.

Actually, The NCP1631 PWM section does not directly use \[ V_{\text{control}} \] but \[ V_{\text{REGUL}} \]. Taking into the \((\frac{5}{9})\) resistors divider that links \[ V_{\text{control}} \] and \[ V_{\text{REGUL}} \], it comes:

\[ \frac{V_{\text{REGUL}}}{V_{\text{out}}} = \frac{1 + s R_z C_z}{s \frac{9}{5} R_z \cdot \left( C_z + C_p \right) \left( 1 + s R_z \frac{C_z \cdot C_p}{C_z + C_p} \right)} \]

(eq. 46)

Hence, we have:

\[ \frac{V_{\text{REGUL}}}{V_{\text{out}}} = \frac{1 + \frac{s}{2 \pi \cdot f_z}}{\frac{s}{2 \pi \cdot f_p} \left( 1 + \frac{s}{2 \pi \cdot f_{p1}} \right)} \]

(eq. 47)

Where:

- \( f_z \) is the frequency of the compensator zero:

\[ f_z = \frac{1}{2 \pi \cdot R_z \cdot C_z} \]

- \( f_{p1} \) is the frequency of the compensator high frequency pole:

\[ f_{p1} = \frac{1}{2 \pi \cdot R_z \cdot \left( \frac{C_p \cdot C_z}{C_p + C_z} \right)} \]

\[ f_0 \] is the frequency of the origin pole:

\[ f_0 = \frac{5}{18 \pi \cdot R_0 \cdot \left( C_p + C_z \right)} \]

\[ R_0 = \frac{V_{\text{out,nom}}}{V_{\text{ref}} \cdot G_{\text{EA}}} \]

Place the Zero and the High Frequency Pole:

We can obtain a 60° phase boost and hence, a 60° phase margin by placing the compensation zero at \( \left( \frac{f_c}{4} \right) \) and the high frequency pole at \( \left( 4 \times f_c \right) \), where \( f_c \) is the selected crossover frequency.

From this, it comes that:

\[ f_{p1} = 4^2 \cdot f_z \]  

(eq. 48)

Substitution of the \( f_{p1} \) and \( f_z \) expressions into Equation 48 leads to:

\[ \frac{C_p \cdot C_z}{C_p + C_z} = \frac{C_z}{16} \]  

(eq. 49)

Hence:

\[ C_z = 15 \cdot C_p \]  

(eq. 50)

Place the Pole at the Origin to Have the Proper Bandwidth:

Equation 44 instructs that the static gain of the PFC boost is:

\[ G_o = \frac{(R_k)^2 \cdot R_{\text{out}}}{53.8 \cdot 10^{12} \cdot L \cdot k_{BO} \cdot V_{\text{out,nom}}} \]  

(eq. 51)

If \( f_c \) is the desired crossover frequency, the pole at the origin must be placed at the load that would set the boost converter pole at the selected compensation zero.

Hence:

\[ -20 \cdot \log \left( \frac{f_c}{f_0} \right) = -20 \cdot \log \left( G \left( R_{\text{out}} = \frac{4}{\pi \cdot C_{\text{bulk}} \cdot f_c} \right) \right) \]
Computing $R_z$

The compensation zero being placed at $(f_c/4)$, it comes:

$$f_z = \frac{1}{2\pi \cdot R_z \cdot C_z} = \frac{f_c}{4} \quad (eq. 59)$$

Finally, from the above computations, we can deduce the following equations to design the compensation network.

$$C_p = \frac{1.06 \cdot 10^{-6} \cdot (P_{in})_{HL}}{C_{bulk} \cdot f_c^2 \cdot (V_{out,nom})^2} \quad (eq. 60)$$

$$C_z = 15 \cdot C_p \quad (eq. 61)$$

$$R_z = \frac{2}{\pi \cdot C_z \cdot f_c} \quad (eq. 62)$$

In our application,

$$C_p = \frac{1.06 \cdot 10^{-6} \cdot 497}{100 \cdot 10^{-6} \cdot 20^2 \cdot 390^2} \approx 86 \text{ nF} \quad (eq. 63)$$

Practically, we will use 68-nF capacitor that is a close standard value.

$$C_z = 15 \cdot C_p = 1020 \text{ nF} \quad (eq. 64)$$

In practice, a 1-µF standard capacitor is selected. Finally,

$$R_z = \frac{2}{10^{-6} \cdot 20} \approx 31.8 \text{ k}\Omega \quad (eq. 65)$$

A 33-k\Omega resistor is implemented.

The compensation is computed to have a phase margin in the range of 60°. The high frequency pole can be set at a lower frequency. Practically, $C_p$ can be increased up to 4 times the proposed value (without changing $R_z$ and $C_z$) to reduce the ripple on the $V_{control}$ pin and further improve the THD. The crossover frequency is unchanged. This is just at the cost of a diminution of the phase margin that can drop as low as 30°. More specifically:

$$\phi_m = \arctan \left( \frac{f_c}{f_z} \right) - \arctan \left( \frac{f_c}{f_{p1}} \right) \quad (eq. 66)$$

Where:

- $f_z$ is the frequency of the compensator zero:

$$f_z = \frac{1}{2\pi \cdot R_z \cdot C_z}$$

- $f_{p1}$ is the frequency of the compensator high frequency pole:

$$f_{p1} = \frac{1}{2\pi \cdot R_z \cdot \left( \frac{C_p \cdot C_z}{C_p + C_z} \right)}$$

Finally, a 150-nF capacitor is selected for $C_p$, leading to:

$(f_z \approx 5 \text{ Hz}), \ (f_{p1} \approx 37 \text{ Hz}), \ (\phi_m \approx 76^\circ - 28^\circ = 48^\circ)$
The CS block performs the over-current protection and detects the in-rush currents.

Figure 8. Current Sense Block
The NCP1631 is designed to monitor a negative voltage proportional to the coil current. Practically, a current sense resistor \( R_{CS} \) of Figure 8 is inserted in the return path to generate a negative voltage proportional to the total current absorbed by the two branches. The circuit incorporates an operational amplifier that sources the current necessary to maintain the CS pin voltage null (refer to Figure 8). By inserting a resistor \( R_{OCP} \) between the CS pin and \( R_{CS} \), we adjust the pin9 current as follows:

\[- (R_{CS} \cdot I_{p9}) + (R_{OCP} \cdot I_{pin9}) = V_{p9} \approx 0 \quad (eq. 67)\]

Which leads to:

\[ I_{CS} = I_{pin9} = \frac{R_{CS}}{R_{OCP}} I_{in} \quad (eq. 68) \]

Where \( I_{in} \) is the total current drawn by the two phases of the interleaved PFC stage.

The circuit compares \( I_{CS} \) to an internal 210-\( \mu \)A current reference for a cycle by cycle current limitation. Hence, the maximum coil current is:

\[ I_{in,max} = \frac{R_{OCP}}{R_{CS}} \cdot 210 \mu A \quad (eq. 69) \]

Finally, the ratio \( \frac{R_{OCP}}{R_{CS}} \) sets the over-current limit in accordance with the following equation:

\[ \frac{R_{OCP}}{R_{CS}} = \frac{I_{in,max}}{210 \mu A} \quad (eq. 70) \]

As we have two external components to set the current limit \( R_{OCP} \) and \( R_{CS} \), the current sense resistor can be optimized to have the best trade-off between losses and noise immunity.

- Maximum current drawn by the two branches:

  As shown in [1], the following equations give the total current that is absorbed by the interleaved PFC.

\[ I_{in,max} = 2 \cdot \sqrt{2} \cdot \left( \frac{P_{in,avg}}{V_{in, rms}} \right)_{LL} \cdot 4 \cdot V_{out,nom} \left( \frac{V_{in, rms}}{2 \cdot V_{out,nom}} \right) \]

\[ I_{in,max} = 2 \cdot \sqrt{2} \cdot \left( \frac{P_{in,avg}}{V_{in, rms}} \right)_{LL} \cdot 4 \cdot V_{out,nom} \left( \frac{V_{in, rms}}{2 \cdot V_{out,nom}} \right) \]

Where:

\( (V_{in, rms})_{LL} \) is the lowest level of the line rms voltage.

\( (P_{in, avg})_{max} \) is the maximum level of the input power.

\( V_{out,nom} \) is the nominal level of the output voltage (or the output regulation voltage)

In our case,

\[ (V_{in, rms})_{LL} = 90 \leq \frac{V_{out,nom}}{2 \cdot 2} = \frac{390}{4 \cdot 2} = 31.2 \]

Hence:

\[ I_{in,max} = 2 \cdot \sqrt{2} \cdot 325 \cdot \left[ 1 - \frac{390}{4 \cdot (390 - (\sqrt{2} \cdot 90))} \right] \approx 6.4 A \quad (eq. 74) \]

Finally:

\[ R_{CS} = \alpha \cdot \frac{(V_{in, rms})_{min}^2}{(P_{in, avg})_{max}} \quad (eq. 77) \]

And:

\[ R_{OCP} = R_{CS} \cdot \frac{I_{in,max}}{210 \mu A} \quad (eq. 78) \]

Generally (\( \alpha = 0.2\%) \) gives a good trade-off between losses and noise immunity (0.2% of the power is lost in the \( R_{CS} \) at low line).
This criterion leads to the following $R_{CS}$ value:

$$R_{CS} = 0.2\% \cdot \frac{90^2}{325} \approx 50 \, \text{m\Omega} \quad \text{(eq. 79)}$$

This selection results in the following $R_{OCP}$ resistor:

$$R_{OCP} = 50 \, \text{m\Omega} \cdot \frac{6.4 \, \text{A}}{210 \, \text{\muA}} \approx 1.5 \, \text{k\Omega} \quad \text{(eq. 80)}$$

### ZERO CURRENT DETECTION (ZCD)

For each phase, a winding taken off of the boost inductor gives the zero current detection (ZCD) information. When

$$V_{ZCD} = -\frac{V_{in}}{N} \quad \text{(eq. 81)}$$

Where $V_{in}$ is the instantaneous ac line voltage and $N$, the turns ratio (ratio number of turns of the primary winding over the number of turns of the ZCD auxiliary winding)

When the switch is off, the ZCD pin voltage is equal to:

$$V_{ZCD} = \frac{V_{out} - V_{in}}{N} \quad \text{(eq. 82)}$$

The NCP1631 incorporates two ZCD comparators:

1. A first one senses pin 1 that is to receive the ZCD voltage from branch 2
2. A second one monitors pin16 that receives the ZCD signal for branch 1.

The ZCD comparators have a 0.5-V threshold (rising, with a 250-mV hysteresis). Therefore, $N$ must be sized such that at least 0.5 V is obtained on the ZCD pin during the demagnetization in all operating conditions. The voltage obtained on the ZCD pin is minimal in high line and at the top of the sinusoid, leading to:

$$N \leq \frac{V_{out} - \left(\sqrt{2} \cdot (V_{in,\text{rms}})_{HL}\right)}{0.5}$$

With $((V_{in,\text{rms}})_{HL} = 265 \, \text{V})$ and $V_{out} = 390 \, \text{V}$, $N$ must be lower than 30. A turns ratio of 10 was selected for this design.

A resistor, $R_{ZCD1}$, is to be added between the phase 1 ZCD winding and pin 16 for branch 1 and another one $R_{ZCD2}$ between the phase 2 ZCD winding and pin1 for branch 2. $R_{ZCD1}$ and $R_{ZCD2}$ limit the current into or out of pins 1 and 16. This current is preferably set in the range of 2 mA (sink and source). In general, the pins are the most stressed by the sink current obtained at high line. Hence, $R_{ZCD1}$ and $R_{ZCD2}$ must be selected high enough so that:

$$R_{ZCD1} = R_{ZCD2} \geq \frac{\sqrt{2} \cdot (V_{in,\text{rms}})_{HL}}{I_{ZCD} \cdot N} \quad \text{(eq. 83)}$$

A 22-kΩ was selected.

However, the value of this resistor and the small parasitic capacitance of the ZCD pin also determine when the ZCD winding information is detected and the next drive pulse begins. Ideally, the ZCD resistor will restart the drive at its valley. This will minimize switching losses by turning the MOSFET back on when its drain voltage is at a minimum. The value of $R_{ZCD1}$ and $R_{ZCD2}$ to accomplish this is best found experimentally. Too high of a value could create a significant delay in detecting the ZCD event. In this case, the controller would operate in discontinuous conduction mode (DCM) and the power factor would suffer. Conversely, if the ZCD resistor is too low, then the next driver pulse would start when the voltage is still high and switching efficiency would suffer.

### OVER-VOLTAGE PROTECTION

The NCP1631 dedicates one specific pin for the under-voltage and over-voltage protections. The NCP1631 configuration allows the implementation of two separate feed-back networks (see Figure 10):

- One for Regulation Applied to Pin 4 (Feed-back Input)
- Another One for the OVP Function

---

Figure 9. Configuration with One Feed-back Network for Both OVP and Regulation

Figure 10. Configuration with Two Separate Feed-back Networks

Figure 11. Another Configuration with Two Separate Feed-back Networks
The double feed-back configuration offers some redundancy and hence, an up-graded safety level as it protects the PFC stage even if there is a failure of one of the two feed-back arrangements.

However, the regulation and the OVP function have the same reference voltage (VREF = 2.5 V) so that if wished, one single feed-back arrangement is possible as portrayed by Figure 9. The regulation and OVP blocks having the same reference voltage, the resistance ratio Rout2 over Rout3 adjusts the OVP threshold. More specifically,

- The bulk regulation voltage is:
  \[ V_{out,nom} = \frac{R_{out1} + R_{out2} + R_{out3}}{R_{out2} + R_{out3}} \cdot V_{REF} \quad \text{(eq. 84)} \]
- The (bulk) OVP level is:
  \[ V_{out,ovp} = \frac{R_{out1} + R_{out2} + R_{out3}}{R_{out2}} \cdot V_{REF} \quad \text{(eq. 85)} \]
- The ratio OVP level over regulation level is:
  \[ \frac{V_{out,ovp}}{V_{out,nom}} = 1 + \frac{R_{out3}}{R_{out2}} \quad \text{(eq. 86)} \]

For instance, \( R_{out3} = 5\% \times R_{out2} \) leads to \( V_{out,ovp} = 105\% \times V_{out,nom} \).

As soon and as long as the circuit detects that the output voltage exceeds the OVP voltage, the power switch is turned off to stop the power delivery.

In our application, the option that consists of two separate Vout sensing networks is chosen (configuration of Figure 10). Like for the regulation network, the impedance of the monitoring resistors must be:

1. High enough to limit the losses that if excessive, may not allow to comply with the stand-by requirements to be met by most power supplies
2. Low enough for a good noise immunity

Again, a bias current in the range of 100 \( \mu \)A generally gives a good trade-off.

Hence:
\[ R_{ovp2} = \frac{V_{ref}}{100 \mu A} = 25 \text{ k}\Omega \quad \text{(eq. 87)} \]

In practice, \( R_{ovp2} = 27 \text{ k}\Omega \) was selected and as a consequence:

\[ R_{ovp1} = R_{ovp2} \cdot \left( \frac{V_{out,ovp}}{V_{REF}} - 1 \right) \quad \text{(eq. 88)} \]

In our application, our 410-V target leads to:
\[ R_{ovp1} = 27 \text{ k}\Omega \cdot \left( \frac{410}{2.5} - 1 \right) = 4401 \text{ k}\Omega \quad \text{(eq. 89)} \]

For safety reason, several resistors should be placed in series instead of a single \( R_{ovp1} \) one. In our application, we choose a \((1,800 \text{ k}\Omega + 1,800 \text{ k}\Omega + 820 \text{ k}\Omega)\) network. The exact OVP level is then:
\[ V_{out,ovp} = \frac{R_{ovp1} + R_{ovp2}}{R_{ovp2}} \cdot V_{REF} \]
\[ = \frac{1800 k + 1800 k + 820 k + 27 k}{27 k} \cdot 2.5 \text{ V} \]
\[ \approx 412 \text{ V} \]

Remark:
As illustrated by Figure 11, another effective means to dimension the OVP sensing network is, to select:

- \( R_{ovp2} = R_{fb2} \)
- \( R_{ovp1} = R_{fb1} + R_{ovp} \), where \( R_{ovp} \) is a part of the upper resistor of the OVP sensing network.

Note that:
\[ V_{out,nom} = \frac{R_{fb1} + R_{fb2}}{R_{fb2}} \cdot V_{REF} \]
\[ V_{out,ovp} = \frac{R_{ovp1} + R_{ovp2}}{R_{ovp2}} \cdot V_{REF} = \]
\[ = \frac{R_{fb1} + R_{ovp} + R_{fb2}}{R_{fb2}} \cdot V_{REF} \]

Combining two precedent equations, it comes:
\[ V_{out,ovp} = V_{out,nom} + \frac{R_{ovp}}{R_{fb2}} \cdot V_{REF} \]

In other words, the OVP protection trips when the overshoot exceeds:
\[ \left( \frac{R_{ovp}}{R_{fb2}} \cdot V_{REF} \right) \]

CONCLUSIONS

This application note proposes a systematic approach for the eased design of an efficient 2-phase, interleaved PFC. More specifically, this paper provides the key equations and design criteria necessary to dimension the PFC stage. The practical implementation of a 300-W, wide mains application illustrates the process.

For detailed information on the performance of a 300-W interleaved PFC designed according to the proposed method, you can refer to NCP1631EVB/D [3]. This application note shows that the efficiency can remain as high as almost 95% at 90 Vrms from 20% to 100% of the load, despite the relatively high switching frequency range that was selected (120-kHz nominal clamp frequency).

The following table summarizes the key equations useful to design a NCP1631 driven interleaved PFC. Another table reports the results of these computations for our 300-W application of interest.

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### Table 1. GENERAL EQUATIONS – SUMMARY

<table>
<thead>
<tr>
<th>Component</th>
<th>Equation</th>
</tr>
</thead>
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| **Coil Selection** | \[
L \geq \frac{(V_{in,rms})_{LL}^2 \cdot (V_{out,nom} - \sqrt{2} \cdot (V_{in,rms})_{LL})}{(P_{in,avg})_{max} \cdot V_{out,nom} \cdot f_{OSC(nom)}} \]
| | \[
(l_{L(pk)})_{max} = \sqrt{2} \cdot \frac{(P_{in,avg})_{max}}{(V_{in,rms})_{LL}} \]
| | \[
(l_{L(rms)})_{max} = \frac{1}{3} \cdot \frac{(P_{in,avg})_{max}}{(V_{in,rms})_{LL}} \]
| **MOSFET Conduction Losses** | \[
(P_{on})_{max} = \frac{1}{3} \cdot R_{DS(on)} \cdot \left(\frac{(P_{in,avg})_{max}}{(V_{in,rms})_{LL}}\right)^2 \cdot \left[1 - \frac{8 \cdot \sqrt{2} \cdot (V_{in,rms})_{LL}}{3\pi \cdot V_{out,nom}}\right] \]
| **Bulk Capacitor** | \[
(\delta V_{out})_{pk-pk} = \frac{P_{out,max}}{C_{bulk} \cdot \omega \cdot V_{out,nom}} \]
| | \[
C_{bulk} \geq \frac{2 \cdot P_{out,max} \cdot t_{HOLD-UP}}{V_{out,nom}^2 - V_{out,min}^2} \]
| | \[
(l_{C,rms})_{max} = \sqrt{\left(\frac{16 \cdot \sqrt{2}}{9\pi} \cdot \frac{(P_{in,avg})_{max}^2}{(V_{in,rms})_{LL} \cdot V_{out,nom}}\right) - (P_{out})_{max}^2} \]
| **Brown-out Block** | \[
R_{bo1} = \frac{(V_{in,avg})_{boH} - \left((V_{in,avg})_{boL} \cdot \left(1 - \frac{f_{BO}}{3\cdot f_{line}}\right)\right)}{I_{HYST}} \]
| **BO Bottom Resistor** | \[
R_{bo2} = \frac{R_{bo1}}{\left(\frac{(V_{in,avg})_{boL}}{V_{BO(th)}} \cdot \left(1 - \frac{f_{BO}}{3\cdot f_{line}}\right)\right) - 1} \]
| **BO Filtering Capacitor** | \[
C_{bo} = \frac{R_{bo1} + R_{bo2}}{2\pi \cdot R_{bo1} \cdot R_{bo2} \cdot f_{BO}} \]
| **Timing Resistor** | \[
R_{t} = 4026 \cdot 10^3 \cdot k_{BO} \cdot \sqrt{(L_{p})_{HL}} \]
| **Oscillator Frequency (No Frequency Foldback)** | \[
(f_{OSC(nom)})_{max} = \frac{52 \cdot 10^{-6}}{C_{OSC}} \]
| | \[
(f_{sw(max)})_{nom} = \frac{f_{OSC(nom)}}{2} = \frac{26 \cdot 10^{-6}}{C_{OSC}} \]
| **Fold-Forward Power Threshold** | \[
(P_{in})_{FF} = \frac{R_{FF}}{15810 \ \Omega} \cdot (P_{in})_{HL} \]
| **Minimum Frequency (per Branch)** | \[
(f_{sw(max)})_{min} = \frac{1}{2 \cdot R_{Fmin} \cdot C_{OSC} \cdot \left(0.22 + \ln\left(\frac{R_{Fmin} - 114000}{R_{Fmin} - 143000}\right)\right)} \]
| **Feedback Resistors** | \[
R_{fb2} = \frac{V_{REF}}{I_{FB}} \]
| | \[
R_{fb1} = R_{fb2} \cdot \frac{V_{out,nom}}{V_{REF}} - 1 \]
Table 1. GENERAL EQUATIONS – SUMMARY (continued)

<table>
<thead>
<tr>
<th>OVP Resistors</th>
<th>OVP Bottom Resistor</th>
<th>R_{ovp2} = \frac{V_{REF}}{I_{FB}}</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>OVP Upper Resistor</td>
<td>R_{ovp1} = R_{ovp2} \cdot \left(\frac{V_{out,ovp}}{V_{REF}} - 1\right)</td>
</tr>
<tr>
<td>Loop Compensation</td>
<td>C_p Capacitor of the Type2 Compensation</td>
<td>C_p = 1.06 \cdot 10^{-6} \cdot \frac{(P_{in})<em>{HL}}{C</em>{bulk} \cdot f_c^2 \cdot (V_{out,nom})^2}</td>
</tr>
<tr>
<td></td>
<td>C_z Capacitor of the Type2 Compensation</td>
<td>C_z = 15 \cdot C_p</td>
</tr>
<tr>
<td></td>
<td>R_z Resistor of the Type2 Compensation</td>
<td>R_z = \frac{2}{\pi \cdot C_z \cdot f_c}</td>
</tr>
</tbody>
</table>

- f_{OSC(nom)} is the oscillator frequency without frequency foldback
- f_{sw(max)} is the nominal clamp frequency for each branch (in the absence of frequency foldback), that is
  \( f_{OSC(nom)} \)
- f_{sw(max)}_{min} is the minimum clamp frequency for each branch resulting from frequency foldback
- V_{out,nom} is the nominal output voltage of the PFC stage (regulation level)
- (V_{in,rms})_{LL} is the lowest level of the line rms voltage
- (P_{in,avg})_{max} is the maximum level of the average input power
- (I_{L, pk})_{max} is the maximum peak current absorbed by one branch of the interleaved PFC (normal operation)
- (I_{L, rms})_{max} is the maximum rms current drawn by one branch of the interleaved PFC (normal operation)
- P_{on} are the MOSFET conduction losses (in one branch)
- R_{DS(on)} is the MOSFET on-time resistor (for one branch)
- (\delta V_{out})_{pk-pk} is the output peak to peak ripple
- \( f_{line} \) is the line frequency
- C_{bulk} is the bulk capacitor
- t_{HOLD-UP} is the specified hold-up time
- (I_{C, rms})_{max} is the rms current of the bulk capacitor. Its given computation assumes a resistive load.
- V_{out, min} is the minimum level of the output voltage that is acceptable for the downstream converter
- (P_{in})_{HL} is the maximum level that can be virtually delivered by the PFC stage as allowed by the timing resistor selection. For the sake of a welcome margin, ((P_{in})_{HL}) should be selected about 30% higher than the expected maximal input power that is:
  \( (P_{in})_{HL} = 130\% \cdot (P_{in, avg})_{max} \)
- (P_{in})_{FF} is the input power level below which the circuit starts to reduce the switching frequency (Frequency Fold-back)
- R_{FF} is the resistor to be placed between pin6 and ground to control the frequency fold-back characteristic
- R_{Fmin} is the resistor that can be placed between the oscillator pin and ground to adjust a minimum frequency. The moderate impact on the f_{OSC(nom)} value

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is not taken into account in the given $f_{OSC(nom)}$ computation equation.

- $R_{p1}$ and $R_{p2}$ are the feedback sensing resistors.
- $R_{ovp1}$ and $R_{ovp2}$ are the OVP sensing resistors.
- $V_{out,ovp}$ is the OVP output voltage.
- $V_{REF}$ is the internal 2.5-V voltage reference.
- $k_{BO}$ is the Brown-out scaling down factor
  $$k_{BO} = \frac{R_{bo2}}{R_{bo1} + R_{bo2}}$$
- $f_{BO}$ is the frequency pole created by the BO pin
- $I_{HYST}$ is the internal 7-% hysteresis
- $V_{BO(th)}$ is the internal 1-V brown-out voltage reference.
- $R_{bo1}$ and $R_{bo2}$ are the Brown-out sensing resistors.
- $V_{out,ovp}$ is the OVP output voltage.
- $R_{ovp1}$ and $R_{ovp2}$ are the OVP sensing resistors.
- $R_{CS}$ is the current sense resistor.

Table 2. EQUATIONS – SUMMARY

<table>
<thead>
<tr>
<th>Power Components</th>
<th>Coils Selection</th>
<th>MOSFET Conduction Losses</th>
<th>Bulk Capacitor</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$L \geq \frac{90^2 \cdot (390 - \sqrt{2} \cdot 90)}{320 \cdot 390 \cdot 120 , \text{k}} \approx 140 , \mu\text{H}$</td>
<td>$(I_{L, pk})_{max} = \sqrt{2} \cdot \frac{320}{90} \approx 5.0 , \text{A}$</td>
<td>$C_{bulk} \geq 2 \cdot \frac{300 \cdot t_{\text{HOLD-UP}}}{390^2 - 330^2} \approx 0.014 \cdot t_{\text{HOLD-UP}}$</td>
</tr>
<tr>
<td></td>
<td>$(I_{L, rms})_{max} = \frac{1}{\sqrt{3}} \cdot \frac{320}{90} \approx 2.1 , \text{A}$</td>
<td>$\langle P_{on} \rangle_{max} = \frac{1}{3} \cdot R_{DS(on)} \cdot \left(\frac{320}{90}\right)^2 \left[1 - \frac{8 \sqrt{2} \cdot 90}{3 \pi \cdot 390}\right] \approx 3 \cdot R_{DS(on)}$</td>
<td>$(I_{c, rms})_{max} = \sqrt{\frac{16 \sqrt{2}}{9 \pi} \cdot \frac{325^2}{90 \cdot 390} - \frac{300}{390}^2} \approx 1.3 , \text{A}$</td>
</tr>
</tbody>
</table>

- $P_{CS}$ are the losses across $R_{sense}$. 0.2% of the maximum power generally gives a good trade-off between noise immunity and efficiency.
- $R_{QCP}$ is the resistor that placed between the CS pin and $R_{CS}$, sets the maximum level of the input current (total current absorbed by the two branches).

Remark Regarding the Compensation:

The compensation is computed to have a phase margin in the range of 60°. The high frequency pole can be set at a lower frequency. Practically, $C_p$ can be increased up to 4 times the proposed value (without changing $R_z$ and $C_z$) to reduce the ripple on the $V_{control}$ pin and further improve the THD. This is at the cost of a diminution of the phase margin that can drop as low as 30°.

Example 1: 300-W, Wide Mains Application

We select a 120-kHz frequency clamp per branch. The maximum output power being 300 W, we estimate that the input power can be as high as around 325 W (92% efficiency at the lowest line – conservative figure that offers some margin). The power capability ($P_{in,HL}$) is set 125% higher at 400 W.

The minimum input voltage being 90 Vrms, the brown-out block is dimensioned so that the circuit starts operating when the line rms voltage exceeds 81 V and a brown-out fault is detected when the line magnitude goes below 72 V.

The regulation level is set to 390 V ($V_{out,nom} = 390 \, \text{V}$) and the OVP level to 410 V ($V_{out,ovp} = 410 \, \text{V}$). A 100-µF bulk capacitor is implemented.

The current resistor is selected so that it does not consume more than about 0.2% of the maximum power ($P_{Rsense} = 0.2% \times (P_{in,avg})_{max}$).
Table 2. EQUATIONS – SUMMARY (continued)

<table>
<thead>
<tr>
<th>Component</th>
<th>Equation</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Brown-out Block</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>BO Upper Resistor</td>
<td>( R_{bo1} = \frac{115 - \left( \frac{65 \cdot \left( 1 - 0% \right)}{3} \right)}{7 \cdot 10^{-6}} \approx 7450 \text{ k\Omega} \Rightarrow 7200 \text{ k\Omega} )</td>
<td></td>
</tr>
<tr>
<td>BO Bottom Resistor</td>
<td>( R_{bo2} = \frac{7200 \cdot 10^3}{\left( \frac{65}{3} \cdot (1 - 0%) \right) - 1} \approx 116 \text{ k\Omega} \Rightarrow 120 \text{ k\Omega} )</td>
<td></td>
</tr>
<tr>
<td>BO Filtering Capacitor</td>
<td>( C_{bo} = \frac{7200 k + 120 k}{2\pi \cdot 7200 k \cdot 120 k \cdot 10% \cdot \frac{f_{\text{line}}}{f_{\text{line}}}} \approx \frac{13.5 \cdot 10^{-6}}{f_{\text{line}}} \approx 220 \text{ nF} ) ( (f_{\text{line}} = 60 \text{ Hz}) )</td>
<td></td>
</tr>
<tr>
<td><strong>Timing Resistor</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Pin3 Resistor</td>
<td>( R_t = \frac{4026 \cdot 10^3 \cdot 120 k}{7200 k \cdot 120 k} \cdot \sqrt{150 \mu \cdot 400} \approx 16.2 \text{ k\Omega} \Rightarrow 18 \text{ k\Omega} \Rightarrow (P_{\text{in}})_{\text{HL}} = 494 \text{ W} )</td>
<td></td>
</tr>
<tr>
<td><strong>Oscillator</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Oscillator Frequency (No Frequency Foldback)</td>
<td>( f_{\text{OSC(nom)}} = \frac{52 \cdot 10^{-6}}{220 \cdot 10^{-12}} \approx 236 \text{ kHz} )</td>
<td></td>
</tr>
<tr>
<td>Clamp Frequency per Branch</td>
<td>( \left( f_{\text{sw(max)}} \right)<em>{\text{nom}} = \frac{f</em>{\text{OSC(nom)}}}{2} \approx 118 \text{ kHz} )</td>
<td></td>
</tr>
<tr>
<td>Fold-Forward Power Threshold</td>
<td>( (P_{\text{in}})<em>{\text{FF}} = \frac{R</em>{\text{FF}}}{15810 \Omega} \cdot (P_{\text{in}})_{\text{HL}} = 4700 \Omega \cdot 494 \approx 147 \text{ W} )</td>
<td></td>
</tr>
<tr>
<td>Minimum Frequency (per Branch)</td>
<td>( \left( f_{\text{sw(max)}} \right)_{\text{min}} = \frac{1}{2 \cdot 270 k \cdot 220 p \cdot \left( 0.22 + \ln \left( \frac{270 k - 114 k}{270 k - 143 k} \right) \right)} \approx 19.8 \text{ kHz} )</td>
<td></td>
</tr>
<tr>
<td><strong>Feedback Resistors</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Feedback Bottom Resistor</td>
<td>( R_{fb2} = \frac{2.5}{92 \mu} \approx 27 \text{ k\Omega} )</td>
<td></td>
</tr>
<tr>
<td>Feedback Upper Resistor</td>
<td>( R_{fb1} = 27 k \cdot \left( \frac{390}{2.5} - 1 \right) \approx 4185 \text{ k\Omega} )</td>
<td></td>
</tr>
<tr>
<td><strong>OVP Resistors</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>OVP Bottom Resistor</td>
<td>( R_{\text{ovp2}} = \frac{2.5}{92 \mu} \approx 27 \text{ k\Omega} )</td>
<td></td>
</tr>
<tr>
<td>OVP Upper Resistor</td>
<td>( R_{\text{ovp1}} = 27 k \cdot \left( \frac{410}{2.5} - 1 \right) \approx 4400 \text{ k\Omega} )</td>
<td></td>
</tr>
<tr>
<td><strong>Loop Compensation</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( C_p ) Capacitor of the Type2 Compensation</td>
<td>( C_p = 1.06 \cdot 10^{-6} \cdot \frac{494}{100 \cdot 10^{-6} \cdot 20^2 \cdot 390^2} \approx 86 \text{ nF} \Rightarrow 68 \text{ nF} )</td>
<td></td>
</tr>
<tr>
<td>( C_z ) Capacitor of the Type2 Compensation</td>
<td>( C_z = 15 \cdot 68 \mu \approx 1.02 \mu \text{F} \Rightarrow 1.0 \mu \text{F} )</td>
<td></td>
</tr>
<tr>
<td>( R_z ) Resistor of the Type2 Compensation</td>
<td>( R_z = \frac{2}{\pi \cdot 1.0 \mu \cdot 20} \approx 31.8 \text{ k\Omega} \Rightarrow 33 \text{ k\Omega} )</td>
<td></td>
</tr>
<tr>
<td><strong>Current Limitation</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Maximum Level of the Input Current</td>
<td>( I_{\text{in,max}} = 2 \sqrt{2} \cdot \frac{325}{90} \left( 1 - \frac{390}{4 \cdot \left( 390 - \left( \sqrt{2} \cdot 90 \right) \right)} \right) \approx 6.4 \text{ A} )</td>
<td></td>
</tr>
<tr>
<td>Current Sense Resistor</td>
<td>( R_{\text{CS}} = \frac{0.22 \cdot 325 \cdot 90^2}{325^2} = 49.8 \text{ m\Omega} \Rightarrow 50 \text{ m\Omega} )</td>
<td></td>
</tr>
<tr>
<td>Over Current Resistor</td>
<td>( R_{\text{OCP}} = \frac{50 \cdot 10^{-3} \cdot 6.4}{210 \cdot 10^{-6}} \approx 1.52 \text{ k\Omega} \Rightarrow 1.5 \text{ k\Omega} )</td>
<td></td>
</tr>
</tbody>
</table>
Figure 12. Application Schematic
REFERENCES

